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## Report

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# Readability Analysis of PISA 2012 Mathematics, Science and Reading Assessments

National Foundation for Educational  
Research (NFER)



# Readability Analysis of PISA 2012 Mathematics, Science and Reading Assessments

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Published in April 2015  
By the National Foundation for Educational Research,  
The Mere, Upton Park, Slough, Berkshire SL1 2DQ  
[www.nfer.ac.uk](http://www.nfer.ac.uk)

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ISBN 978-1-910008-55-3

**How to cite this publication:**

King, D. and Burge, B. (2015). *Readability Analysis of PISA 2012 Mathematics, Reading and Science Assessments*. Slough: NFER.

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# 1 Introduction

This report presents the results of an analysis of the readability of the PISA 2012 mathematics, science and reading assessment stimuli. Readability refers to the ease with which a text or document can be read and the purpose of this analysis was, therefore, to determine whether the readability of PISA 2012 tests is set at an appropriate level for the 15 year olds sitting them.

Analysis was conducted on the stimuli for each of the assessment clusters listed in Table 1 (further details on the development of what PISA measures, PISA scales and proficiency levels are included in the PISA 2012 Assessment and Analytical Framework (OECD, 2013)).

**Table 1 PISA 2012 mathematics, science and reading assessment clusters**

Domain	Assessment cluster
Mathematics	PM1, PM2, PM3, PM4, PM5, PM6A, PM7A
Science	PS1, PS2, PS3
Reading	PR1, PR2, PR3,

## 2 The readability tests

Readability tests are designed to assess the suitability of tests for pupils at particular grade levels or ages. They measure certain features of texts and subject these to mathematical calculations. A number of tests are available and have been developed for different purposes. Most have been developed in the United States and the outcomes are therefore measured with reference to the US grade system. The tests used in this analysis are based on American English but this is not thought to impact significantly on the results.

### 2.1 Readability tests used

The stimuli within each of the assessment clusters for mathematics (PM1,2,3,4,5,6A,7A), science (PS1,2,3) and reading (PR1,2,3) were analysed using the following tests:

- Flesch-Kincaid
- New Dale-Chall
- New Fog Count
- SMOG
- Spache Revised

#### 2.1.1 Flesch-Kincaid

This test is designed to assess the readability of technical documents and is mostly applicable to manuals and forms rather than information books or literary works. This test primarily uses sentence length and syllable count to generate its readability scores.

#### 2.1.2 New Dale-Chall

This test is generally used to help classify school text books and literature for primary and secondary age readers. Sentence length and frequency of unfamiliar words are the main factors in this calculation of readability. The *New Dale-Chall* word list contains 3000 simple familiar words which more than 80 per cent of US 4<sup>th</sup> Grade (Wales Y5, pupils aged 9-10 years) pupils can understand.

As the test is based on the usage of familiar words rather than syllable or letter counts, it is often regarded as a more accurate test of readability for younger readers. It is also considered more appropriate than the *Spache Revised* (see section 2.1.5) for assessing the readability of texts designed for older children because the word list is based on vocabulary familiar to 4<sup>th</sup> Grade pupils (rather than 3<sup>rd</sup> Grade in the case the *Spache Revised*). It should be noted that this test provides a grade *range* rather than a specific grade *point* as identified in the other tests.

### 2.1.3 New Fog Count

This is a modified version of the *Gunning Fog Index* which was created for the US Navy and was designed for technical documents and manuals. The readability score is based on sentence length and the number of words containing three or more syllables, with all numerals and proper nouns being treated as easy words. The index estimates the years of formal education needed to understand the text on a first reading.

### 2.1.4 SMOG

*SMOG*, colloquially known as Simple Measure of Gobbledygook, is generally appropriate for secondary age readers from 4th Grade to college level (Wales Y5 to Y13). *SMOG* tests for 100 per cent comprehension, whereas most readability tests test for around 50 to 75 per cent comprehension. This calculation is based upon sentence length and the number of words consisting of three or more syllables. For the *SMOG* test, numerals are fully syllabised (i.e. sounded out). As is the case for the New Fog Count, *SMOG* estimates the years of education needed in order for a reader to understand a piece of writing and is widely used, particularly for checking general public health messages. It is recommended for use by National Institute of Adult and Continuing Education (NIACE).

### 2.1.5 Spache Revised

This is generally used for primary age readers in the US Kindergarten to 7th grade (in Wales Y1 – Y8) to help classify school books and literature. Factors involved in producing a Spache readability score are sentence length and the proportion of unique unfamiliar words. The *Spache Revised* (1974) word list contains 1041 words which are considered familiar to pupils in the 3<sup>rd</sup> Grade (Welsh Y4, pupils aged 8-9 years) or below.

At the outset, it was considered that the *Spache Revised* might not be the most appropriate readability test for this stimuli and the decision was taken to reassess after analysis. Previous investigation of the outcomes suggests that it may suffer from a ceiling effect and, as the word list is based on words which are recognisable by pupils in US 3<sup>rd</sup> Grade (Wales Y4) and below, there is a limit to the usefulness of these given that it does not take account of the vocabulary that could be expected of 15 year old pupils (the PISA target population). This is supported by the fact that the *Spache Revised* readability measure consistently produces reading ages lower than the other readability tests.

Of the other tests, the *New Fog Count*, based on *Gunning Fog Index*, is the least applicable test for use when analysing PISA texts. This is because it was created for the US Navy and designed for technical documents and manuals and therefore has a different target population to those being assessed with the PISA materials. Similarly, the results of the *Flesch-Kincaid* and *SMOG* tests, both of which only analyse word and sentence length, are also of limited use. We recommend that greater weight is placed upon the outcomes of the *New Dale-Chall* test as it was devised to analyse the readability of school books and literature and is therefore most closely aligned to

the purpose of this analysis. However, this test does have its own limitations which should be borne in mind when considering the data.



## 2.2 Limitations of readability analyses

It is important to note that:

1. The readability tests have all been designed for different purposes (for example, the *New Fog Count* is adapted from a test created for the US Navy to analyse their technical documents and manuals). Of the five tests, the *New Dale-Chall* and *Spache Revised* were both designed with primary aged children in mind. The *New Dale-Chall* is more accurate for children at the older end of the primary school range, whilst the *Spache Revised* is better suited to younger children (US 3<sup>rd</sup> Grade / Wales Y4) and below.
2. Many of the tests used take into consideration 'unfamiliar' words when they calculate the readability scores. This does not take into account the fact that these words may be explained as part of the text, either in text or through the use of a glossary.
3. Readability analysis does not take into account the design of the text, but rather it assumes plain text with no illustrations, diagrams etc. However, many of the PISA texts include illustrations, diagrams, tables etc.
4. In order to generate meaningful results, readability tests require a minimum of 300 words. Some of the PISA reading and science stimuli and nearly all of the mathematics stimuli contain fewer than 300 words. For this reason, the stimuli for mathematics were analysed in clusters, rather than as individual texts.

### 3 Results of readability tests

Initial findings indicated that readability scores of the *Spache Revised* were significantly lower than those of the other tests. As this was artificially depressing the mean grade level and reading level scores, and considering the concerns raised about the test in section 2.1.5, the decision was taken to remove the *Spache Revised* scores from the analysis.

The grade levels and reading ages for each stimulus, as computed by the *Flesch-Kincaid*, *New Dale-Chall*, *New Fog Count*, and *SMOG* tests, are reported in Tables 3 to 9. Also shown in these tables is the mean grade level and reading age and the word count for each question stimulus. Grade levels given are in years and months. These are US levels so results should be read in conjunction with the conversion information in Table 2 below. As noted above, the mathematics stimuli were analysed in clusters as many of the individual question stimuli contained 30 words or less.

**Table 2 Conversion table for US grade levels and Welsh year groups**

<b>Grade levels (US)</b>	<b>Year groups (Wales)</b>
3	4
4	5
5	6
6	7
7	8
8	9
9	10
10	11
11	12
12	13

### 3.1 Mathematics Stimuli

**Table 3 Readability analysis scores of PM1, 2, 3, 4, 5, 6A, 7A mathematics stimuli\***

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PM1	863	7.4	12.0	5-6	10.0	7.8	12.0	13.0	18.0	8.4	13.0
PM2	1193	7.4	12.0	5-6	10.0	7.1	12.0	10.0	15.0	7.5	12.3
PM3	978	9.9	14.0	7-8	12.0	10.2	15.0	13.0	18.0	10.2	14.8
PM4	821	8.9	13.0	7-8	12.0	8.8	13.0	13.0	18.0	9.6	14.0
PM5	1212	9.5	14.0	9-10	14.0	10.4	15.0	14.0	19.0	10.9	15.5
PM6A	1040	9.2	14.0	7-8	12.0	10.3	15.0	12.0	17.0	9.8	14.5
PM7A	1165	7.8	12.0	7-8	12.0	8.1	13.0	10.0	15.0	8.4	13.0

\*Mathematics stimuli has been analysed as whole clusters rather than individual items.

The results of this analysis shows that the mean reading age required to access the PISA mathematics stimuli ranges from 12.3 to 15.5 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 10 and 14 years.

### 3.2 Science stimuli

**Table 4 Readability analysis scores of PS1 science stimuli**

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PS269	267	10.5	15.0	9-10	14	9.3	14.0	12.0	17.0	10.3	15.0
PS408	449	5.7	10.0	5-6	10.0	5.8	10.0	8.0	13.0	6.3	10.8
PS521	272	5.8	10.0	7-8	12.0	5.1	10.0	7.0	12.0	6.4	11.0
PS519	308	12.0	16.0	13-15	18.0	11.0	16.0	13.0	18.0	12.5	17.0
PS527	494	8.0	13.0	7-8	12.0	6.2	11.0	10.0	15.0	7.9	12.8
PS466	353	6.9	11.0	5-6	10.0	6.2	11.0	9.0	14.0	6.9	11.5

The results of this analysis shows that the mean reading age required to access the PISA PS1 science stimuli ranges from 10.8 years to 17 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 10 and 18 years.

**Table 5 Readability analysis scores of PS2 science stimuli**

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PS326	513	8.0	13.0	7-8	12.0	8.3	13.0	11.0	16.0	8.7	13.5
PS256	48	3.4	8.0	3.0	8.0	2.3	7.0	5.0	10.0	3.4	8.3
PS478	368	10.9	15.0	7-8	12.0	8.4	13.0	11.0	16.0	9.5	14.0
PS413	298	12.7	17.0	7-8	12.0	10.1	15.0	14.0	19.0	11.1	15.8
PS498	393	9.5	14.0	7-8	12.0	8.4	13.0	12.0	17.0	9.4	14.0
PS425	465	9.4	14.0	7-8	12.0	8.3	13.0	12.0	17.0	9.4	14.0

The results of this analysis shows that the mean reading age required to access the PISA PS2 science stimuli ranges from 8.3 to 15.8 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 8 and 12 years.

**Table 6 Readability analysis scores of PS3 science stimuli**

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PS465	349	11.8	16.0	9-10	14.0	11.9	16.0	14.0	19.0	11.8	16.3
PS131	328	10.1	15.0	9-10	14.0	11.5	16.0	13.0	18.0	11.0	15.8
PS428	281	12.2	17.0	9-10	14.0	8.5	13.0	13.0	18.0	10.8	15.5
PS514	400	12.4	17.0	11-12	16.0	13.5	18.0	14.0	19.0	12.9	17.5
PS438	349	11.2	16.0	11-12	16.0	9.9	14.0	13.0	18.0	11.4	16.0
PS415	349	9.3	14.0	9-10	14.0	7.4	12.0	10.0	15.0	9.0	13.8

The results of this analysis shows that the mean reading age required to access the PISA PS3 science stimuli ranges from 13.8 to 17.5 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 14 and 16 years.

### 3.3 Reading stimuli

**Table 7 Readability analysis scores of PR1 reading stimuli**

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PR424	586	10.2	15.0	9-10	14.0	10.1	15.0	13.0	18.0	10.7	15.5
PR404	920	9.4	14.0	7-8	12.0	9.2	14.0	12.0	17.0	9.6	14.3
PR406	670	6.9	11.0	5.6	10.0	6.9	11.0	9.0	13.0	6.9	11.3
PR455	357	10.8	15.0	9-10	14.0	9.0	13.0	13.0	18.0	10.6	15.0

The results of this analysis shows that the mean reading age required to access the PISA PR1 reading stimuli ranges from 11.3 to 15.5 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 10 and 14 years.

**Table 8 Readability analysis scores of PR2 reading stimuli**

Text Code	Word Count	Flesch-Kincaid Grade Level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PR420	367	11.4	16.0	7-8	12.0	11.9	16.0	11.0	16.0	10.5	15.0
PR453	628	7.6	12.0	5-6	10.0	6.8	11.0	10.0	15.0	7.5	12.0
PR412	608	9.6	14.0	7-8	12.0	6.4	11.0	12.0	17.0	8.9	13.5
PR437	431	7.2	12.0	4.0	9.0	6.0	11.0	10.0	15.0	6.8	11.8

The results of this analysis shows that the mean reading age required to access the PISA PR2 reading stimuli ranges from 11.8 to 15 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 9 and 12 years.



**Table 9 Readability analysis scores of PR3 reading stimuli**

Text Code	Word Count	Flesch-Kincaid Grade level	Flesch-Kincaid Reading Age	New Dale-Chall Grade Level	New Dale-Chall Reading Age	New Fog Count Grade Level	New Fog Count Reading Age	SMOG Grade Level	SMOG Reading Age	Mean Grade Level	Mean Reading Age
PR456	348	5.1	10.0	3.0	8.0	5.4	10.0	7.0	12.0	5.1	10.0
PR466	479	6.9	11.0	5.6	10.0	5.2	10.0	10.0	15.0	6.9	11.5
PR446	109	7.9	12.0	7-8	12.0	4.7	9.0	11.0	16.0	7.8	12.3
PR432	423	7.5	12.0	5-6	10.0	8.2	13.0	9.0	14.0	7.6	12.3
PR220	598	9.0	14.0	7-8	12.0	7.7	12.0	12.0	17.0	9.0	13.8

The results of this analysis shows that the mean reading age required to access the PISA PR3 reading stimuli ranges from 10 to 13.8 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required as between 8 years and 12 years.

## 4 Conclusions and recommendations

This report presents an analysis of the PISA 2012 mathematics, science and reading assessment stimuli using four different readability tests. The findings are considered separately for each domain.

### 4.1 Mathematics

The mathematics stimuli was analysed as complete clusters because most of the individual stimuli contained less than 30 words. The results of this analysis using the *Flesch-Kincaid*, *New Dale-Chall*, *New Fog* and *SMOG* readability tests showed that the mean reading age required to access the PISA mathematics stimuli ranges from 12.3 to 15.5 years. The *New Dale-Chall* test, thought to be the most suitable test for this data, calculates the mean reading age required to be between 10 and 14 years. We would conclude from this analysis, therefore, that the readability of the PISA 2012 mathematics tests is at an appropriate level for the 15 year olds sitting them.

### 4.2 Science

#### 4.2.1 Science cluster PS1

For the PS1 science stimuli, results of this analysis using all four readability tests showed that the mean reading age required to access the PISA science stimuli ranges from 10.8 years to 17 years. The *New Dale-Chall* test calculates the mean reading age required to be between 10 and 18 years. On closer examination, item PS519 was the only stimulus requiring a reading age of over 15 years. We would recommend, therefore, that this is taken into consideration when interpreting scores for this question.

#### 4.2.2 Science cluster PS2

The results of the analysis for PS2 using all four readability tests show that the mean reading age required to access the PISA science stimuli ranges from 8.3 to 15.8 years. The *New Dale-Chall* test calculates the mean reading age required to be between 8 and 12 years. This is a large range of scores and, whilst the readability level is accessible for those taking the test, some items are clearly much easier to read than others, in particular item PS256.

#### 4.2.3 Science cluster PS3

For the PS3 stimuli, the results of this analysis using all four readability tests show that the mean reading age required to access the PISA science stimuli ranges from 13.8 to 17.5 years. The *New Dale-Chall* test calculates the mean reading age required to be between 14 and 16 years. Items PS514 and PS438 both require a reading age of over 15 years and therefore we would recommend that that this is taken into consideration when interpreting scores for these questions.

## 4.3 Reading

### 4.3.1 Reading cluster PR1

For PR1, the results of this analysis using the four readability tests show that the mean reading age required to access the PISA reading stimuli ranges from 11.3 to 15.5 years. The *New Dale-Chall* test calculates the mean reading age required to be between 10 and 14 years. We would conclude from this analysis, therefore, that the readability level of the PR1 PISA 2012 reading tests is at an appropriate level for the 15 year olds who are sitting them

### 4.3.2 Reading cluster PR2

For PR2, the results of this analysis using the four readability tests show that the mean reading age required to access the PISA reading stimuli ranges from 11.8 to 15 years. The *New Dale-Chall* test calculates the mean reading age required to be between 9 and 12 years. Again, we would conclude from this that the readability of the PR2 PISA 2012 reading tests is at an appropriate level for the 15 year olds who are sitting them

### 4.3.3 Reading cluster PR3

The results of this analysis using the four readability tests show that the mean reading age required to access the PISA reading stimuli ranges from 10 to 13.8 years. The *New Dale-Chall* test calculates the mean reading age required to be between 8 years and 12 years. Although the readability level is accessible for those sitting the tests, some items are clearly much easier to read than others, in particular item PR456.

## 4.4 Summary

However, results should be interpreted with caution as some readability tests are more suitable for analysing this type of data than others and consideration should also be given to the limitations of the readability analysis. It must also be remembered that readability analysis does not take into account the design of the text, but rather it assumes plain text with no illustrations, diagrams etc. Many of the PISA texts include illustrations, diagrams, tables etc. Furthermore, in order to generate meaningful results, readability tests require a minimum of 300 words. One of the Reading texts (PR446) and three of the Science texts (PS521, PS 428, PS413) contain less than 300 words and the results for these must, therefore, be regarded as less reliable than those for longer texts.

## References

- Dale, E. and Chall, J.S. (1995). *Readability Revisited: the New Dale-Chall Readability Formula*. Northampton, MA: Brookline Books.
- Kincaid, J.P., Fishburne, R.P., Rogers, R.L. and Chissom, B.S. (1975). *Derivation of New Readability Formulas (Automated Readability Index, Fog Count and Flesch Reading Ease Formula) for Navy Enlisted Personnel* (Research Branch Report 8-75). Memphis, TN: Naval Air Station [online]. Available: <http://www.dtic.mil/dtic/tr/fulltext/u2/a006655.pdf> [1 August, 2014].
- McLaughlin, H. (1969). 'SMOG grading - a new readability formula', *Journal of Reading*, **22**, 639–646.
- Spache, G. (1953). 'A new readability formula for primary-grade reading materials', *The Elementary School Journal*, **55**, 410–413.
- Spache, G. (1974). *Good Reading for Poor Readers*. Champaign, ILL: Garrard Publishing Company.

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NFER ref. PQUK ISBN. 978-1-910008-55-3

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